

# Harmonic Oscillator

## Introduction

Harmonic oscillatory movement describes movement in which an object that has been displaced from its point of equilibrium is acted upon by a restoring force directly proportional to the amount of displacement. The classic model of such a movement is a weight attached to a spring, oscillating between the two extremes of maximum compression and maximum extension. In a simple (ideal) system as described, no energy is lost and the weight will oscillate for an infinite amount of time between the two extremes <sup>[1]</sup>. Based on these principles, the position, velocity, and acceleration of such a weight can be modeled by sinusoidal equations, as demonstrated below <sup>[2]</sup>.

## Equations

Equations used to model simple harmonic oscillation in the case of a spring include:

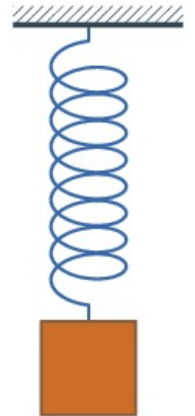
- Restoring force:  $F = -k \cdot x$

$k$  is the spring constant;  $x$  is the displacement from position of equilibrium;  $F$  is the restoring force <sup>[1]</sup>

- Position of the body:  $y = A \cdot \sin(\omega \cdot t + \varphi)$

$y$  is position relative to the point of origin;  $A$  is maximum elongation;  $\omega$  is angular frequency (given by  $\omega = 2 \cdot \pi \cdot f = (2 \cdot \pi) / T$ );  $T$  is the time to make one full oscillation;  $\varphi$  is the phase difference which gives the position of the body at  $T = 0$  and its direction <sup>[2]</sup>

- Maximum velocity:  $V_{\max} = A \cdot \omega$  <sup>[3]</sup>
- Instantaneous velocity:  $V = V_{\max} \cdot \cos(\omega \cdot T)$  <sup>[3]</sup>



Simple harmonic oscillator - example

## Links

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### Bibliography

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